

Find, without use of a calculator or computer, the value of A_{2009} given that $A_0 = 2009$ and

$$A_{n+1} = \frac{A_n}{1 + nA_n}, \quad n = 0, 1, 2, \dots$$