

Prove that for any odd positive integer  $n$ , the number

$$1^n + 2^n + \cdots + n^n$$

is a multiple of  $n^2$ .