

Prove that the positive number  $x$  is rational if and only if the sequence

$$x, x + 1, x + 2, x + 3, \dots$$

contains three (not necessarily consecutive) terms that form a geometric progression.