

Each positive integer is assigned one of three colors. Prove that no matter how this is done, there must always exist a pair of distinct positive integers x and y such that x and y have the same color and $|x - y|$ is a perfect square.