

Evaluate the following limit:

$$\lim_{n \rightarrow \infty} n^{-\frac{1}{2}(1+\frac{1}{n})} (1^1 \cdot 2^2 \cdot 3^3 \cdots n^n)^{\frac{1}{n^2}}.$$