

Is there a sequence $\{a_k\}$ of positive real numbers such that

$$\sum_{k=1}^{\infty} \frac{a_k}{k^2} \quad \text{and} \quad \sum_{k=1}^{\infty} \frac{1}{a_k}$$

both converge? Justify your answer.