

For each permutation  $a_1, a_2, \dots, a_{20}$  of the integers  $1, 2, \dots, 20$ , form the sum

$$|a_1 - a_2| + |a_3 - a_4| + \cdots + |a_{19} - a_{20}|.$$

Find the average value of all such sums.